

# Spectral information content analysis of ISMAR frequencies – Preliminary results

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# Overview

- Optimal estimation theory, reduction of degree of freedom
- ICON model
- 2-moment microphysics
- Jacobian calculation with ARTS
- Jacobians
- Apriori and retrieval error covariances
- Error reduction
- Information content

# Optimal estimation theory

- Mathematical framework for estimation of information content:  
Reduction of degree of freedom

Analysis error covariance **S<sub>r</sub>**

$$S_r = (S_a^{-1} + K^T S_y^{-1} K)^{-1}$$

- K : Jacobian
- S<sub>y</sub> : Measurement error
- S<sub>x</sub> : Apriori covariance

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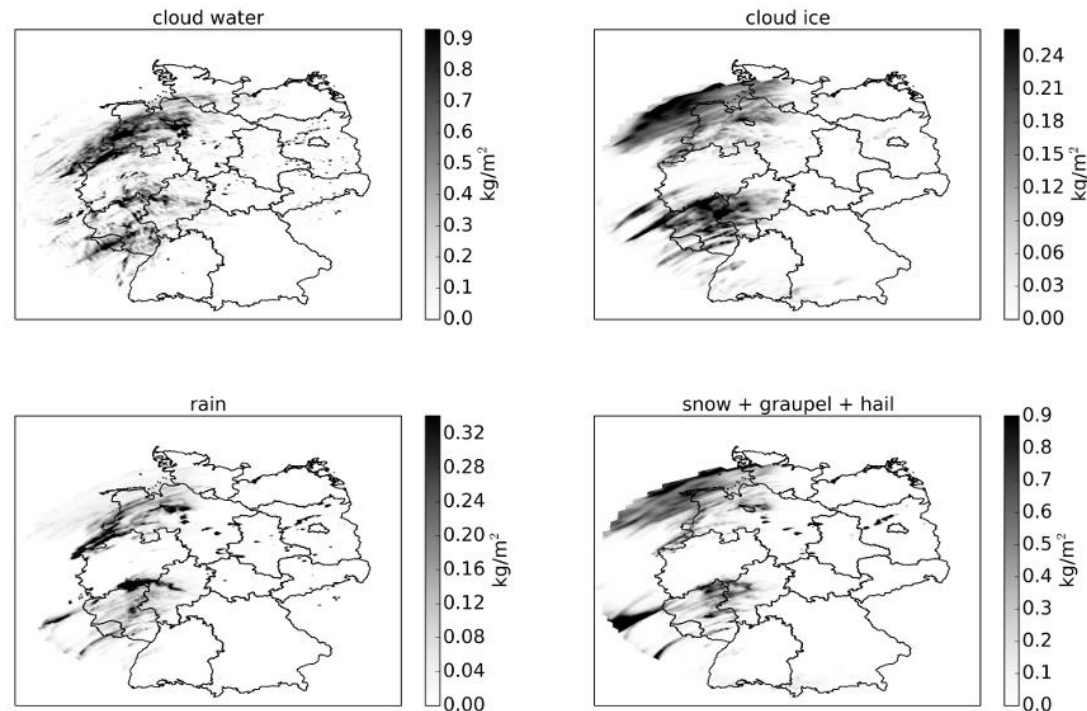
Reduction of degree of freedom:

$$\Delta\text{DOF} = \text{tr} \left( I - \frac{S_r}{S_x} \right)$$

# Model data

- ICON (ICOsahedral Non-hydrostatic model, developed by German Weather Service, DWD, and Max-Planck-Institute for Meteorology)
- Cloud resolving simulation (650m) of a day in April 2013 over Germany

2013-04-26 12:00:00



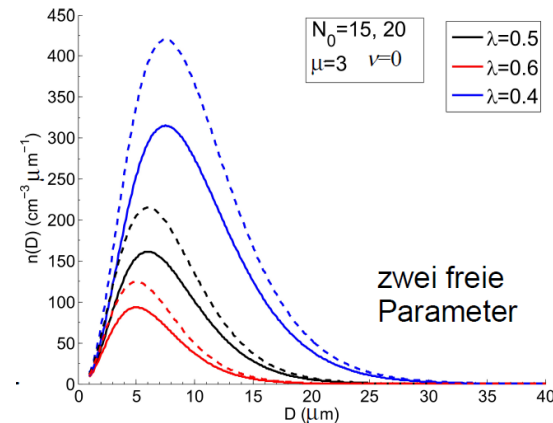
Simulation from project HD(CP)2, <http://hdcp2.eu>

They also have an extensive measurement database for validation.

# Two-moment cloud microphysics

- Hydrometeors represented by mass and number density

- Cloud liquid water (LWC)
- Cloud ice(IWC)
- Rain (RWC)
- Snow (SWC)
- Graupel and hail (not considered here)

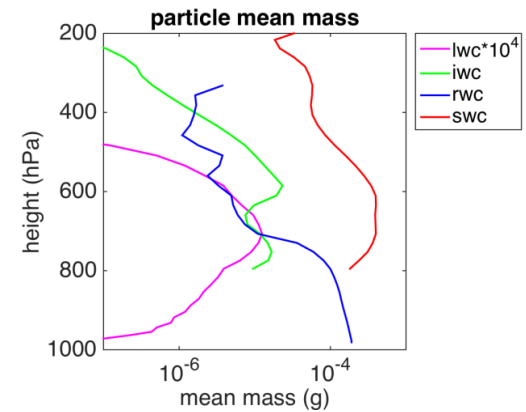
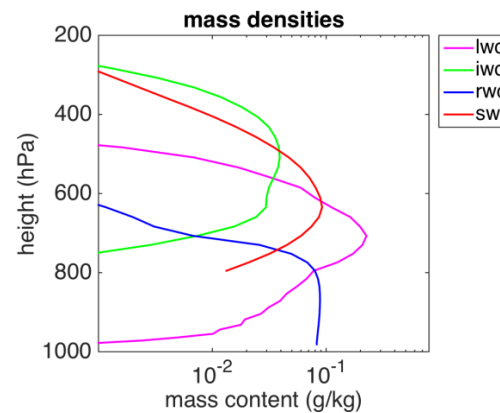
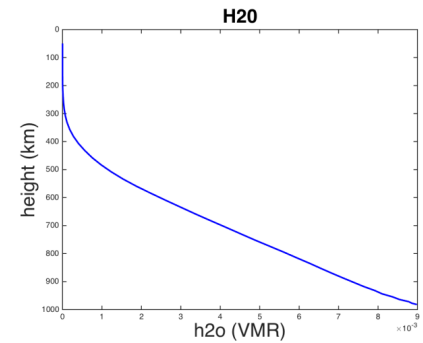
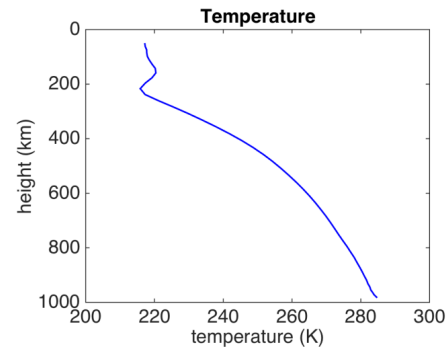


- Modified gamma distribution  $f(m) = A m^\nu \exp(-\lambda m^\mu)$
- $\mu$  and  $\nu$  fixed per hydrometeor,  $A$  and  $\lambda$  calculated from mass and number
- Mean Particle mass by division of grid box mass density by number density

Seifert, A. and Beheng, K. D. (2006). A two-moment cloud microphysics parameterization for mixed-phase clouds. Part 1: Model description. Met. Atm. Phys., 92:45–66

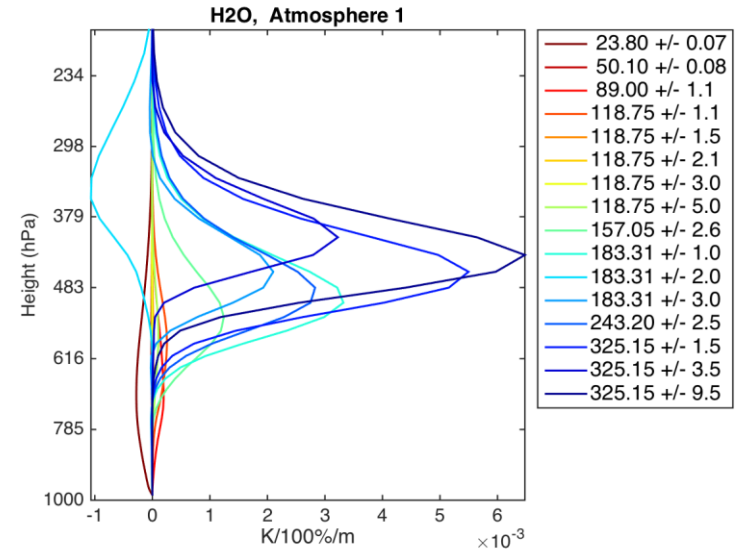
# Atmospheric profile

- Mean atmospheric profile from cloudy gridpoints
- Recalculated mean particle mass from mean mass density and mean number density
- → Smooth profile with all hydrometeors
- Removed cold particles at warm temperatures



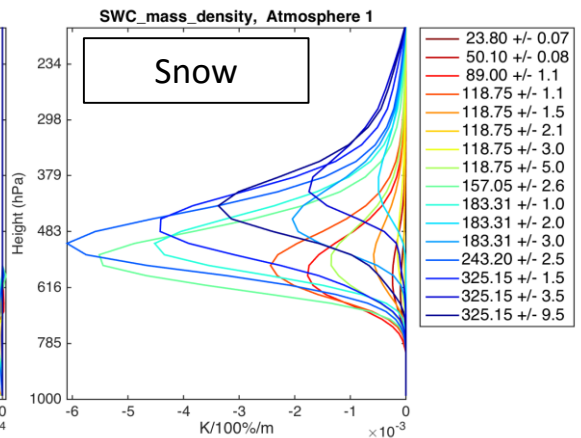
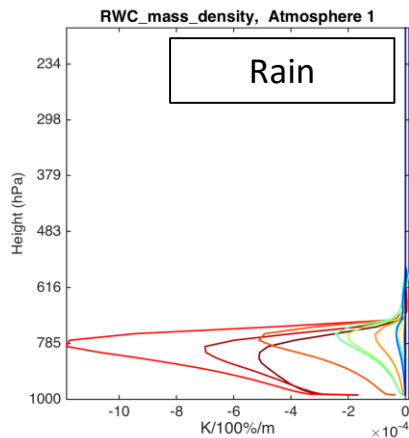
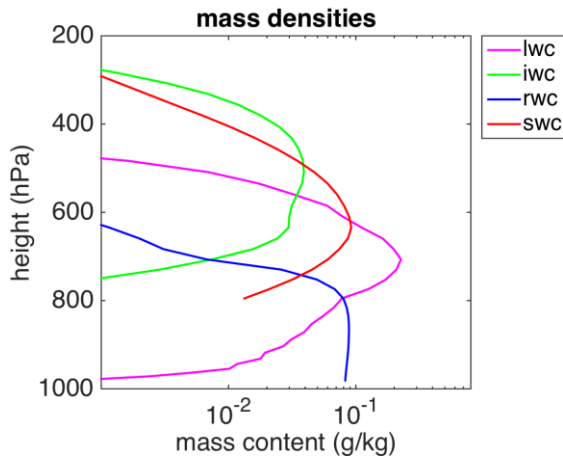
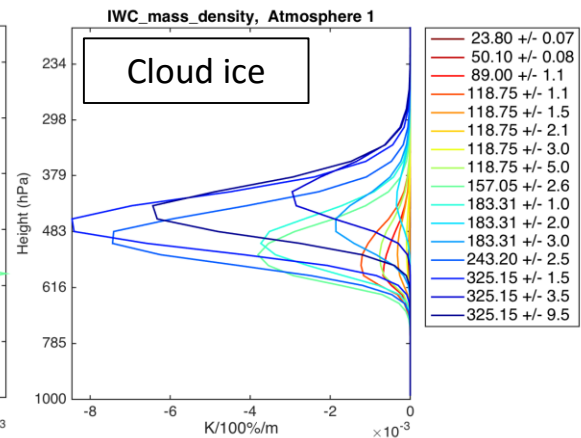
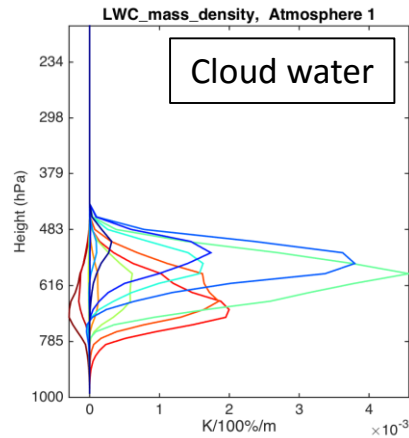
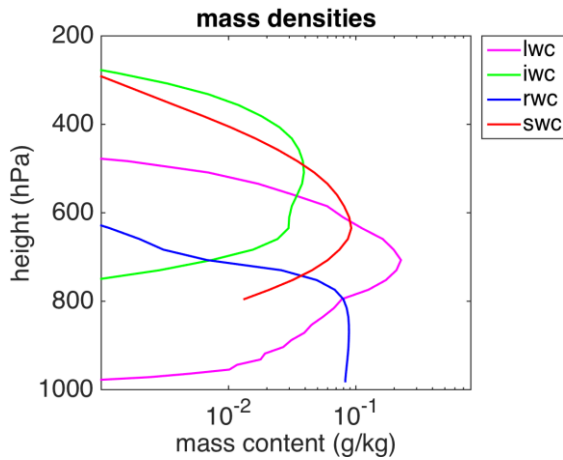
# Jacobian calculation in ARTS

- Line-by-line model, explicit calculation of scattering (more from Jana and Patrick)
- Discretization of the particle size distribution on the ARTS particle size grid for scattering, slight adjustment of the particle number to preserve mass density
- Relative perturbation of 1% on each model level for humidity and hydrometeors → corresponds to retrieval in logarithmic (ln) space
- Frequency set used : 23.8GHz up to 325.15GHz (higher frequencies underway)

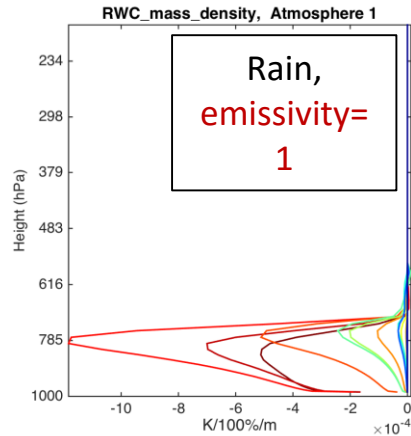
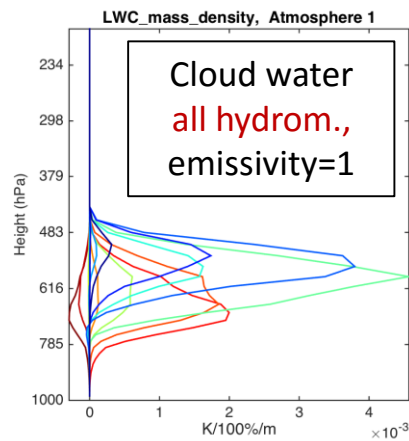
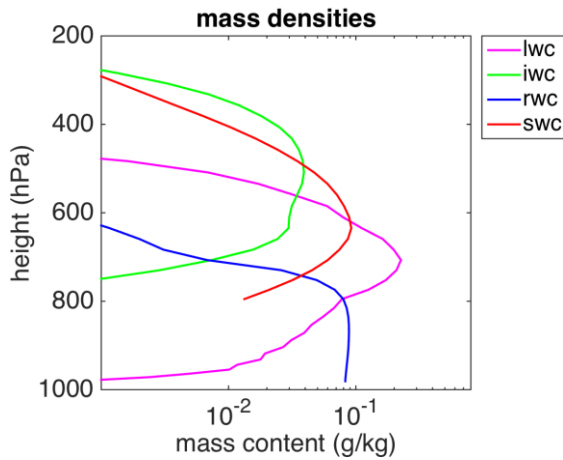




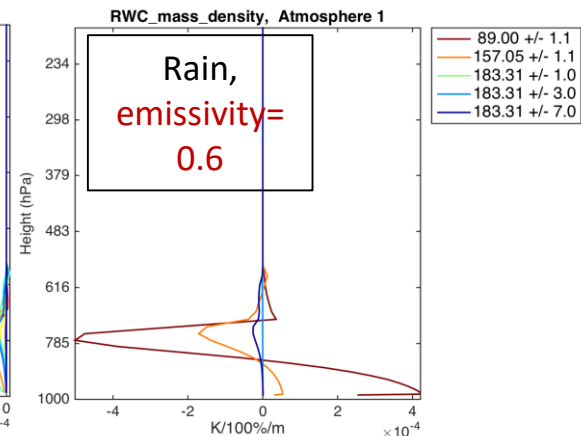
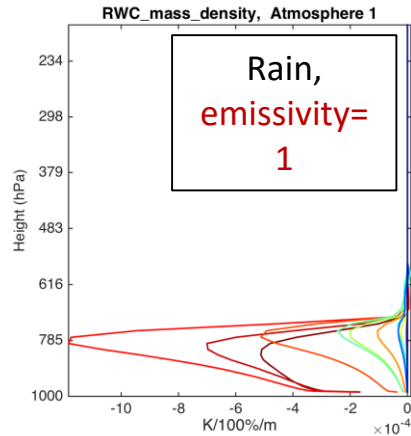
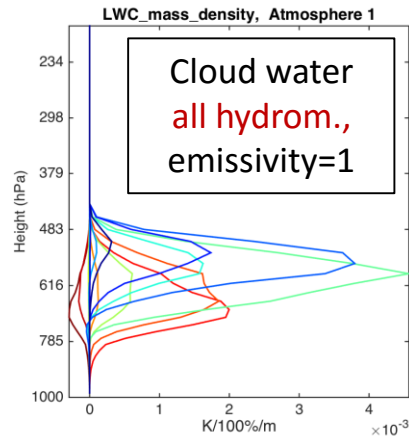
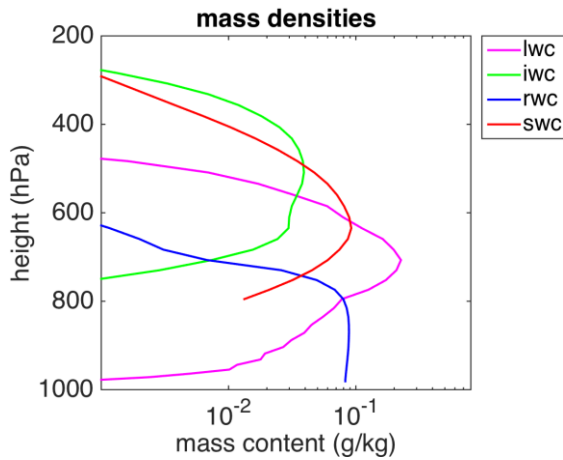
# Jacobians Mass Densities



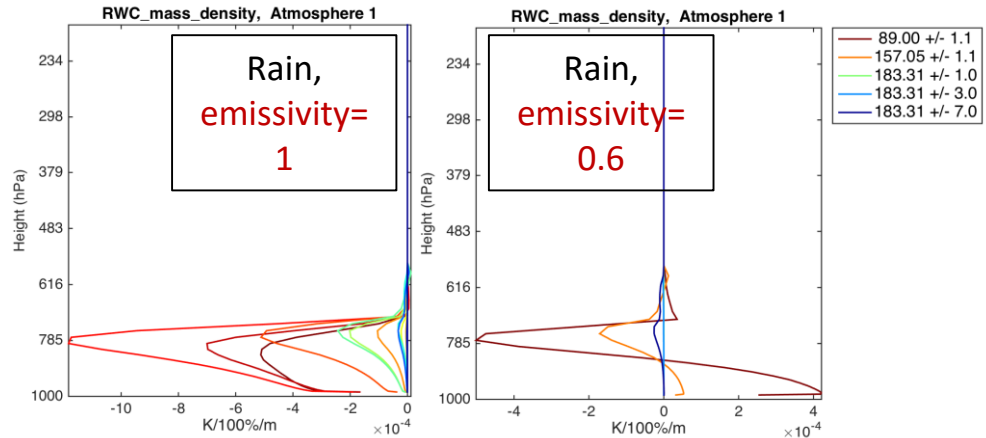
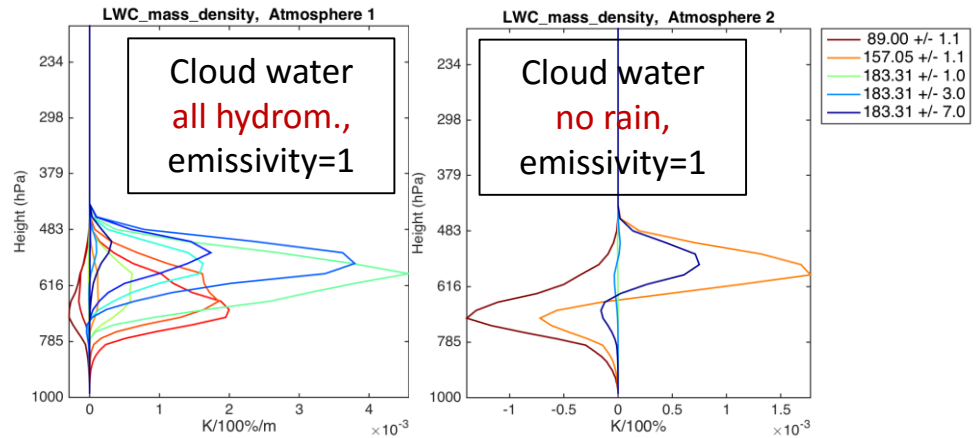
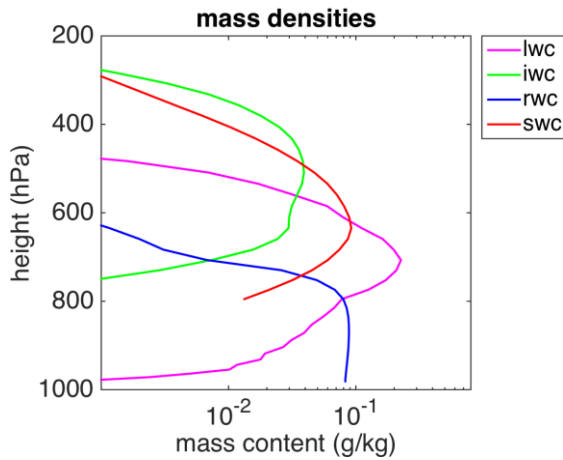
# Jacobians Mass Densities - excursus



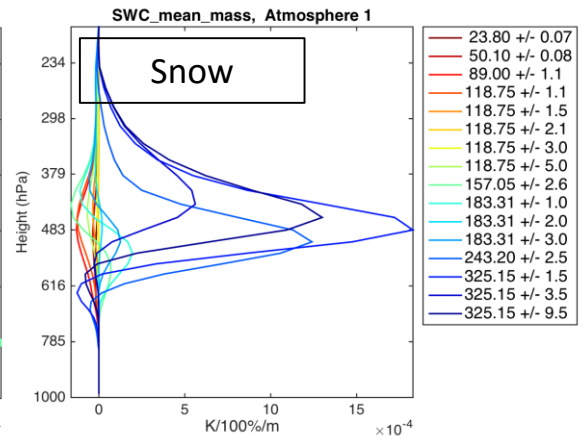
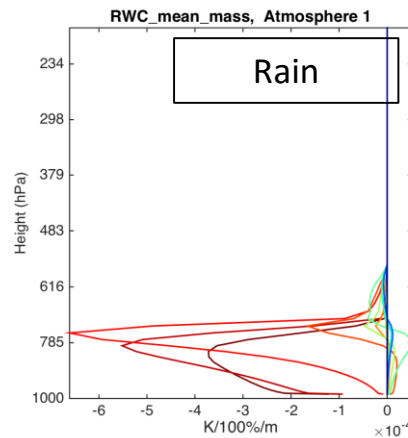
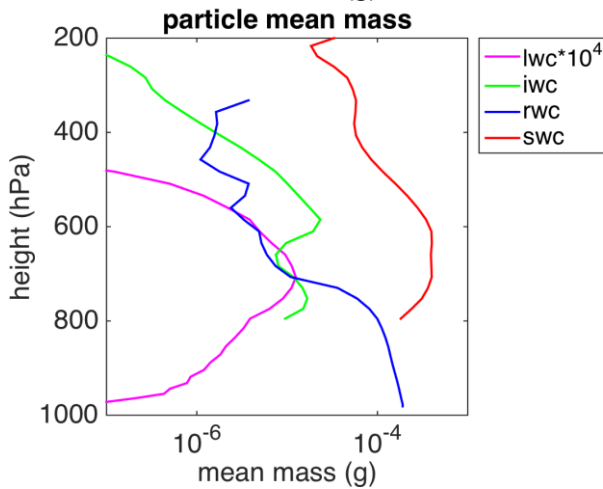
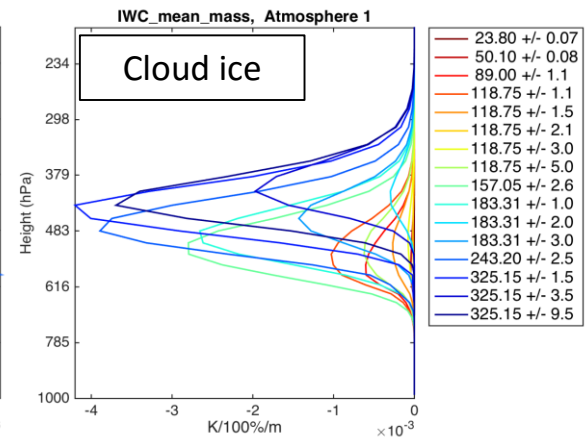
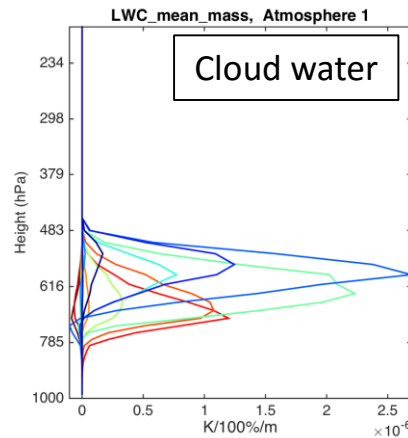
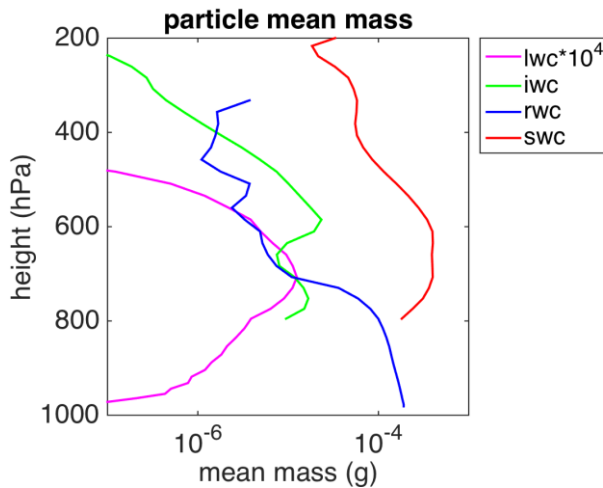
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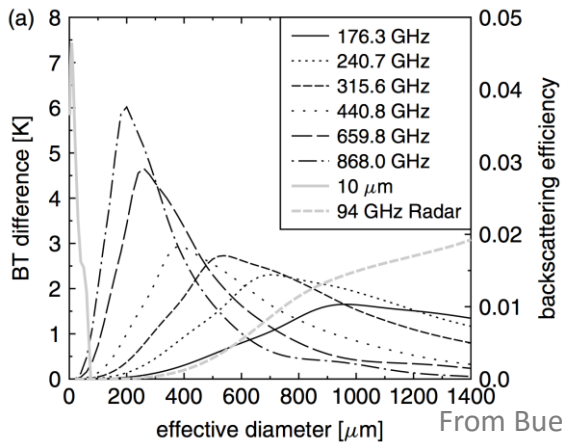
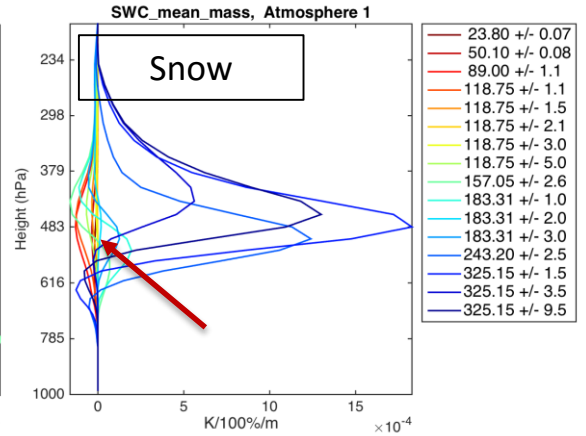
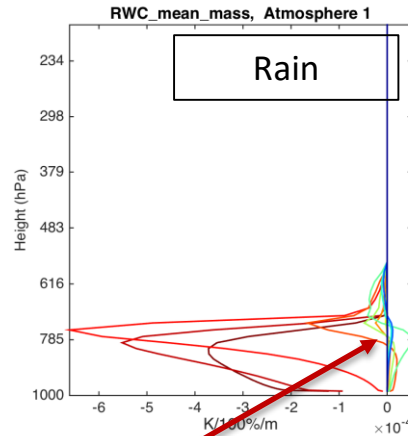
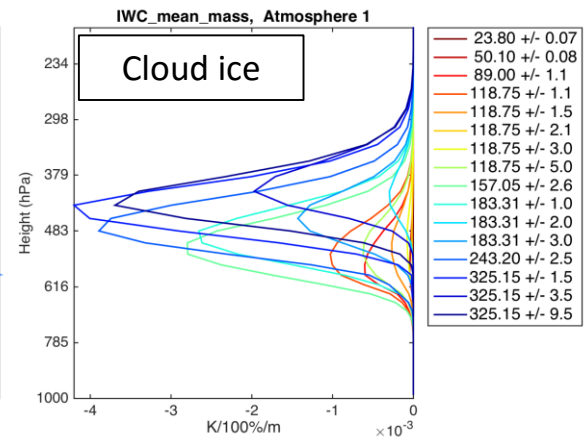
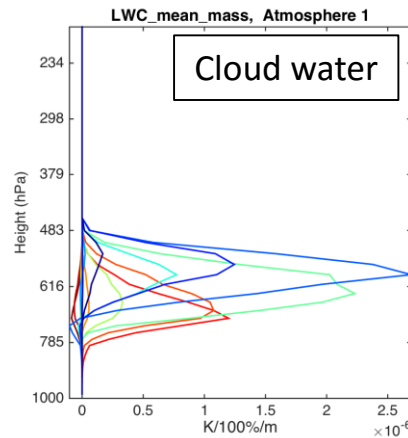
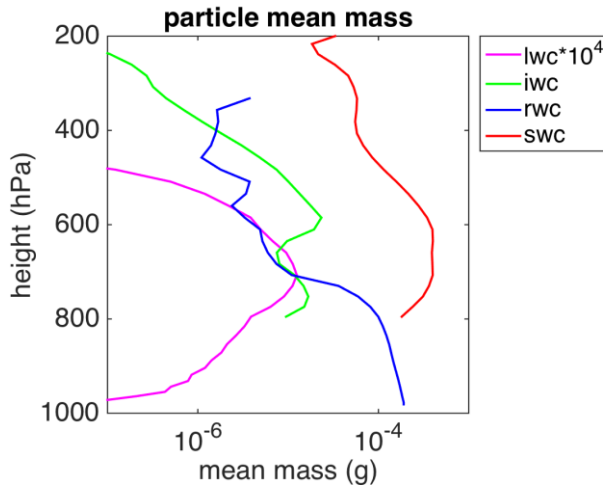
# Jacobians Mass Densities - excursus



# Jacobians Mean Masses



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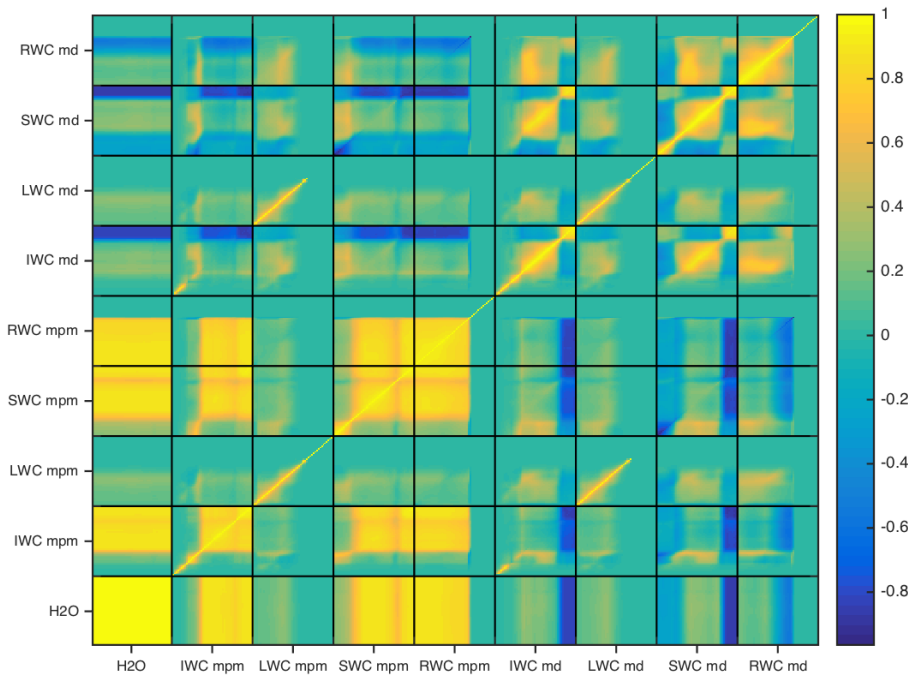


From Buehler et al., 2007. A concept for a satellite mission to measure cloud ice water path and particle size. Q. J. R. Meteorol. Soc. (133), 109-128.

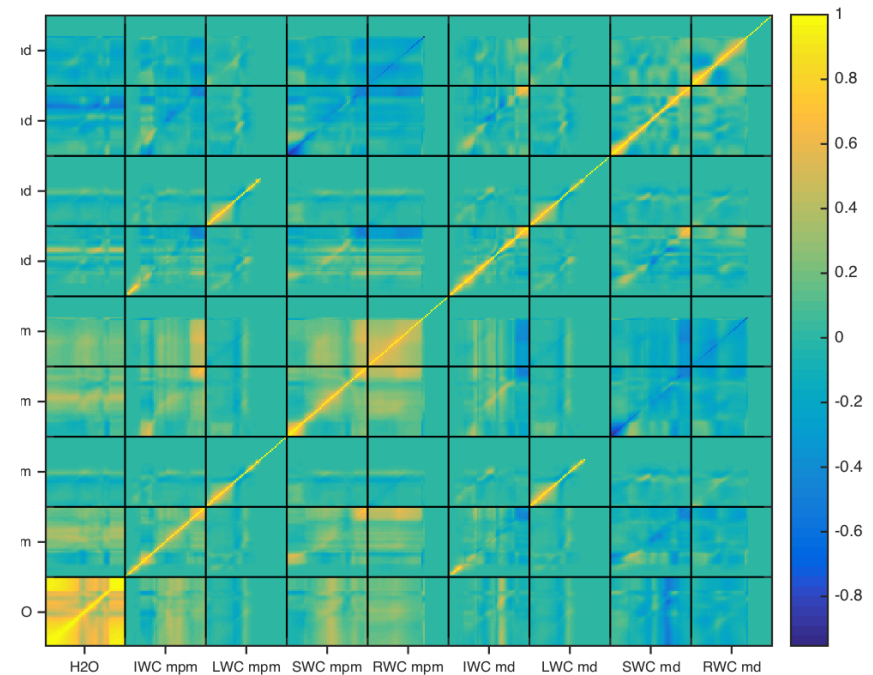
# Apriori and analysis error covariance - ICON

- The initial correlations remain clearly visible but again are “diffused” through out the matrix and overall weakened

Correlation apriori covariance

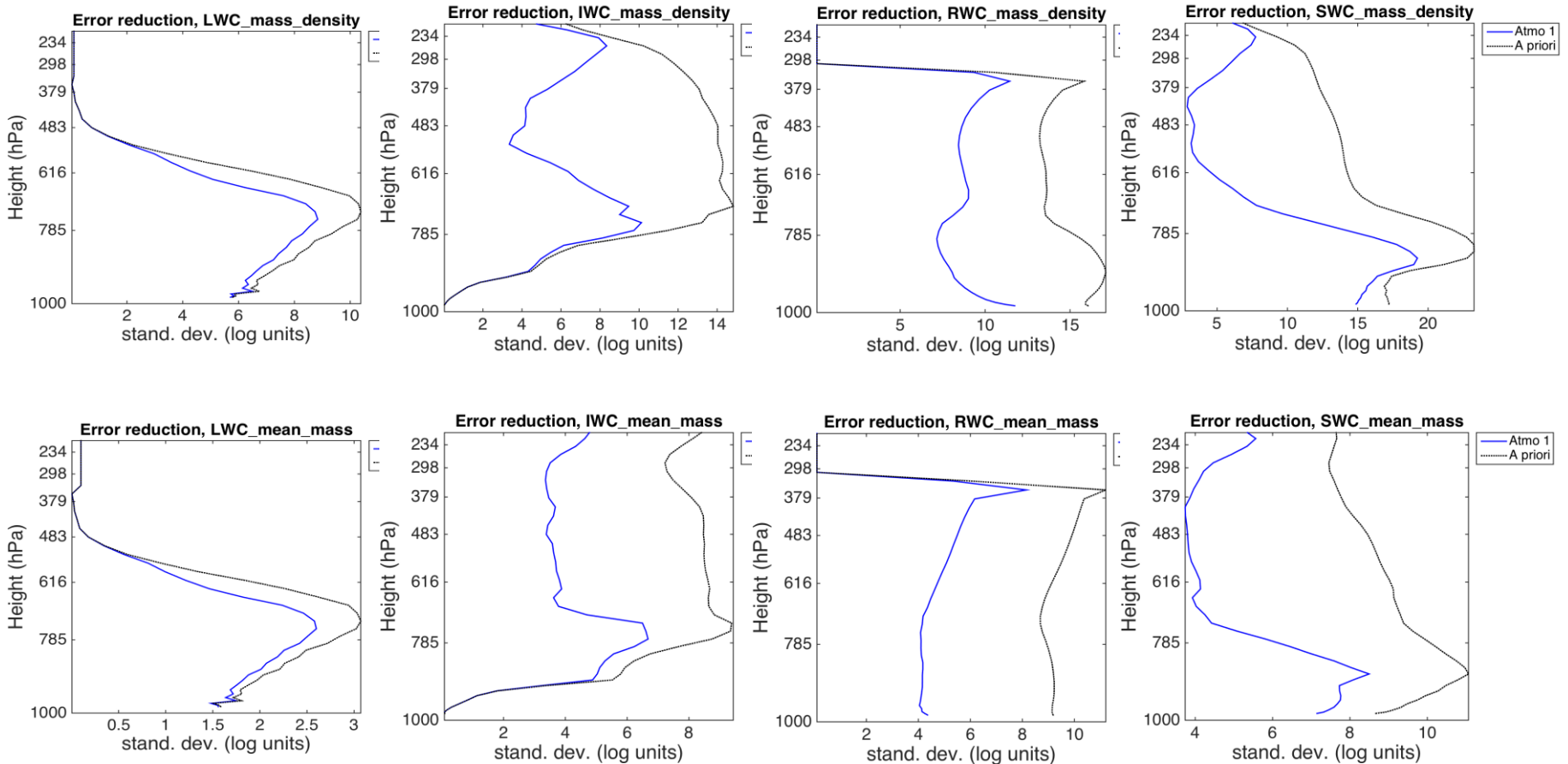


Correlation analysis error covariance



# Error reduction for the ICON case

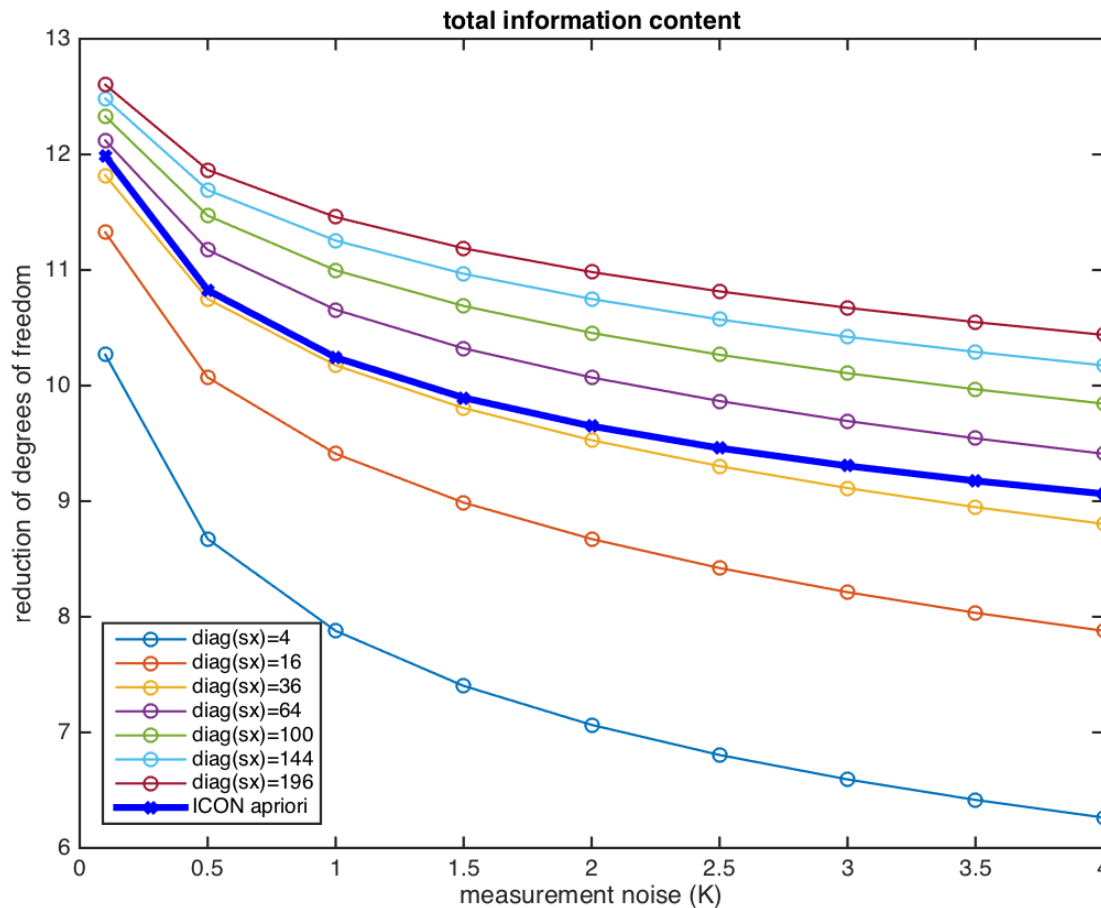
- (Reminder: Square root of the diagonals of  $S_x$  and  $S_r$ )



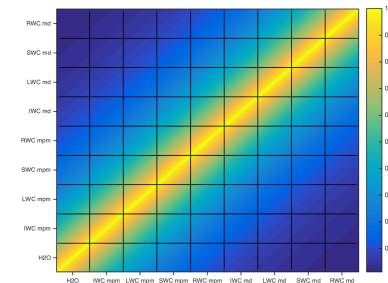


# Information - excursus

- Caveat: absolute number of  $\Delta$ DOF depends on a priori and measurement noise assumptions



Thin lines from idealized a priori of this form:



# Information content

- Example ICON a priori, 0.5K noise
- Total reduction of degree of freedom less than number of measurements
- Hardly information about mean masses (inclusion of higher frequencies likely improves it)
- Breakdown of the information content: how much can we potentially learn about the hydrometeors with this specific setup

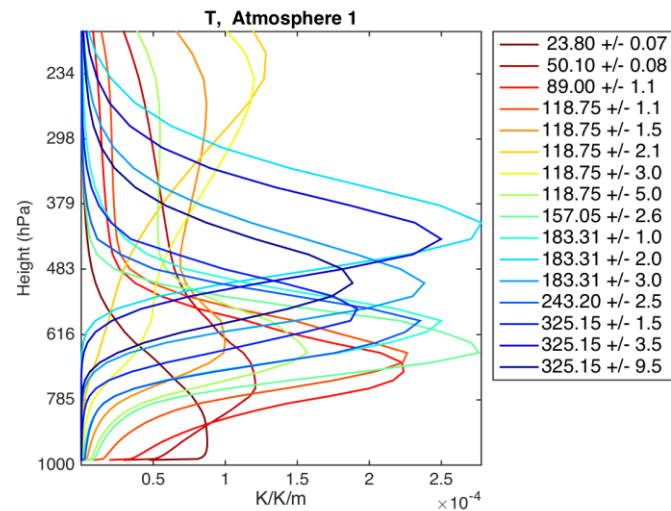
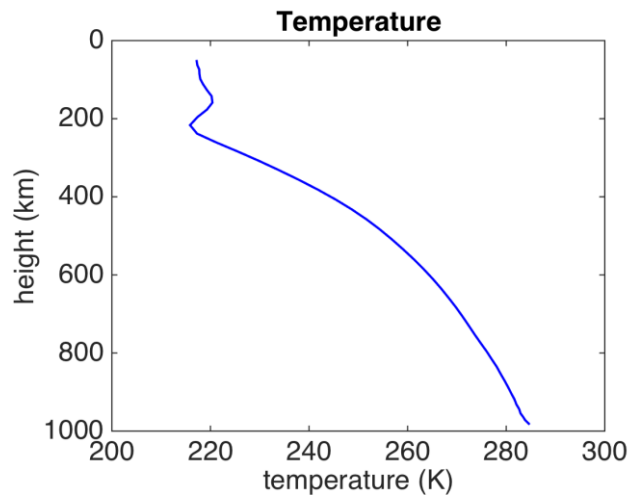
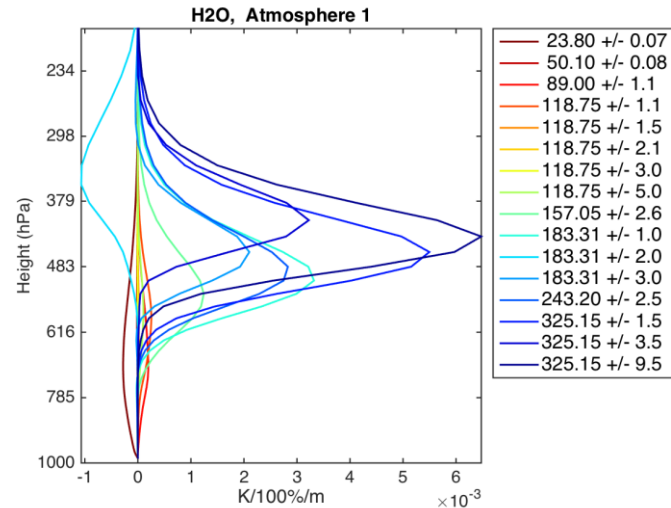
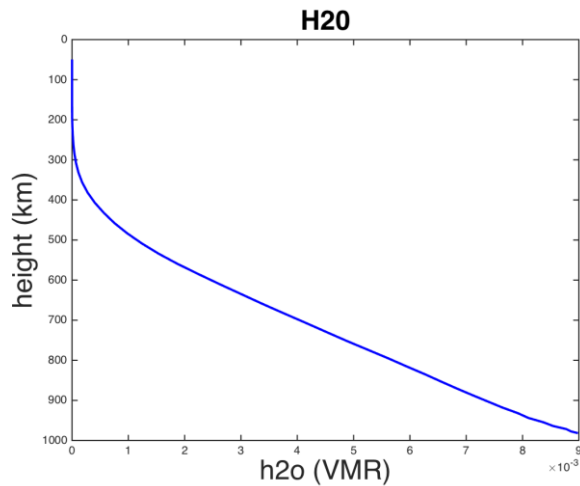
<b>Total reduction of degree of freedom: 10.8256</b>	<b>Contribution</b>
SWC mass density	2.81
mean mass	0.29
IWC mass density	2.67
mean mass	0.35
LWC mass density	2.15
mean mass	3.29e-04
RWC mass density	1.15
mean mass	0.16

# Conclusions

- OEM information content analysis performed for ISMAR frequencies up to 325GHz (higher frequencies underway)
- Two-moment cloud microphysical scheme, estimation of apriori covariance from underlying ICON data
- Jacobian calculations within ARTS, cloudy Jacobians tricky and highly dependent on parameters and cloudy profile
- Reduction of degrees of freedom: How much can we learn about which parameter?

# Backup slides

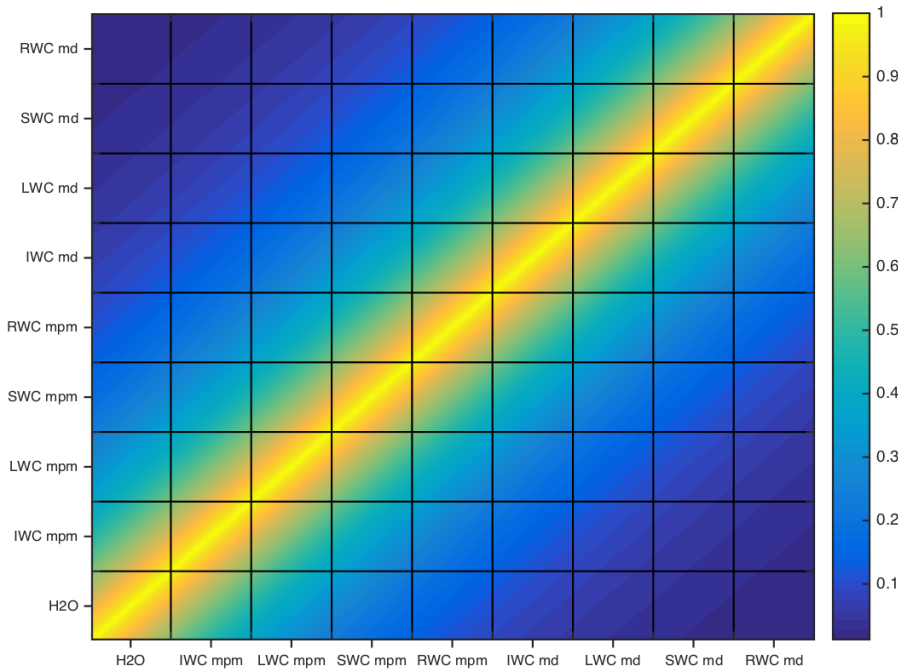
# Jacobians T and H2O



# Apriori and analysis error covariance - ideal

- The initial correlations are “diffused” through out the matrix, new patterns occur

Correlation apriori covariance



Correlation analysis error covariance

